The redshift evolution of the baryonic Tully–Fisher relation in SIMBA

M. Glowacki,^{1,2 \star} E. Elson^{\square 2} and R. Davé^{\square 2,3,4}

¹Inter-University Institute for Data Intensive Astronomy, Bellville 7535, South Africa

²Department of Physics and Astronomy, University of the Western Cape, Robert Sobukwe Road, Bellville 7535, South Africa

³Institute for Astronomy, Royal Observatory, University of Edinburgh, Edinburgh EH9 3HJ, UK

⁴South African Astronomical Observatories, Observatory, Cape Town 7925, South Africa

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ABSTRACT

The baryonic Tully–Fisher relation (BTFR) is an important tool for constraining galaxy evolution models. As 21-cm H I emission studies have been largely restricted to low redshifts, the redshift evolution of the BTFR is less studied. The upcoming LADUMA survey (Looking At the Distant Universe with the MeerKAT Array) will address this. As preparation for LADUMA, we use the SIMBA hydrodynamical galaxy formation simulation from the SIMBA-hires $(25 h^{-1} \text{Mpc})^3$ run to generate rotational velocity measures from galaxy rotation curves (V_{flat}) and H I spectral line profile widths (W_{50} and W_{20}) at three different redshifts (z = 0, 0.5, and 1). Using these measures, together with the dark matter velocity dispersion and halo mass, we consider the redshift evolution of the BTFR of SIMBA galaxies. We find that LADUMA will be successful in detecting weak redshift evolution of the BTFR, provided that auxiliary data are used to distinguish galaxies with discy morphologies. W_{20} spectral line widths give lower scatter and more pronounced redshift evolution compared to W_{50} . We also compare these rotational velocity measures to the dark matter velocity dispersion across redshift and galaxy morphology. We find weak redshift evolution between rotational velocity and the dark matter halo mass, and provide fits for estimating a galaxy's dark matter halo mass from H I spectral line widths. This study with SIMBA showcases the importance of upcoming, deep Square Kilometre Array pathfinder surveys such as LADUMA, and provides predictions to compare with the redshift evolution of the BTFR and galaxy dark matter content from H I rotational velocity measures.

Key words: methods: numerical – galaxies: evolution – galaxies: formation – galaxies: general – galaxies: ISM.

1 INTRODUCTION

The relation between the rotation speeds of galaxies and their luminosity, the Tully–Fisher relation (TFR; Tully & Fisher 1977), gives us an important constraint on galaxy assembly history and feedback processes (e.g. Haynes et al. 1999; Sanders & McGaugh 2002; Springob et al. 2007; de Rossi, Tissera & Pedrosa 2010; Ponomareva et al. 2018). For instance, an even tighter version of this relation spanning multiple orders of magnitude, which includes the gas and stars of galaxies (McGaugh 2012), provides evidence for a link between dark matter haloes and the baryonic content of the galaxies associated with them. This relation is called the baryonic TFR (henceforth BTFR).

There are two main methods in observational studies of the BTFR for obtaining the rotational velocity of galaxies through the neutral hydrogen (H I) gas content traced by the 21-cm 'spin-flip' transition. The first applies primarily to local universe studies, where it is viable to spatially resolve the H I content and derive a rotation curve for the galaxy, which in turn provides a rotational velocity depending on one's method of velocity selection. At higher redshifts, current telescopes cannot image galaxies at the spatial resolution required to measure rotation curves. Alternatively, one can use the spectral

* E-mail: marcin@aapt.net.au

line widths of the H I emission profile as a measure for the rotational velocity to study the BTFR. Both methods have been used extensively (e.g. Verheijen & Sancisi 2001; Noordermeer & Verheijen 2007; Gurovich et al. 2010; McGaugh 2012; Zaritsky et al. 2014; Lelli, McGaugh & Schombert 2016; Ponomareva et al. 2017).

The BTFR found from rotation curves and spectral line widths will vary, as demonstrated in Ponomareva et al. (2018) and Lelli et al. (2019). It is thus important to ask: how does using the H I 21-cm spectral line widths compare to the rotation curve velocity values? Moreover, how do these two methods compare to the true velocity dispersion from the dark matter halo component of these galaxies, which the BTFR aims to trace? This is not something that can be easily answered from observations, given the inability to directly observe the dark matter content of galaxies. While a tight relation has been observed between dark matter velocity dispersion and dark matter halo mass (e.g. Zahid, Sohn & Geller 2018), it is unclear whether H I emission studies can sufficiently measure properties of the larger dark matter halo associated with the host galaxy.

Another aspect to consider is the redshift dependence of both the BTFR and the relation between rotational velocity and the dark matter velocity dispersion. This has been examined in simulations; see the review of the literature in Portinari & Sommer-Larsen (2007). Portinari & Sommer-Larsen (2007) used a small sample of simulated disc galaxies (~25) to study the redshift evolution of the *B*-band TFR, and the stellar mass TFR, across redshifts (*z*) of 0, 0.7, and 1. They show in their fig. 6 that the stellar mass TFR redshift evolution is only slight, but do not comment on the baryonic TFR (i.e. including the galaxy gas mass). The Millennium Simulation, plus a semi-analytical model that was used in Obreschkow et al. (2009a) for a much larger sample (3×10^7 galaxies, of various morphologies), showed the redshift evolution of the BTFR in fig. 14, panel (c), between the redshifts (*z*) of 0, 4.89, and 10.07. This study found that galaxies of equal mass rotate significantly faster at higher redshift, based on an analytical description used to generate H I spectra.

It is a different tale with observational studies. There do exist studies of the redshift evolution of the TFR using other measures; for instance, the *B*-band TFR is examined through optical velocity widths in Vogt (2007), and similarly the *B*-, *R*-, and *I*-band TFR in Fernández Lorenzo et al. (2009). These, however, do not specifically consider the BTFR, nor measure it from the H I content traced through the 21-cm transition. Observational large all-sky surveys involving direct detections of H I through 21-cm, such as the H I Parkes All Sky Survey (Meyer et al. 2004) and the Arecibo Legacy Fast Arecibo *L*-Band Feed Array survey (Darling et al. 2011), have been restricted to z < 0.1, hence limiting the ability to study the BTFR redshift evolution, among other properties.

This is set to change with upcoming Square Kilometre Array (SKA) pathfinder telescope surveys that have improved sensitivity and hence will probe to higher redshifts. Examples include the Widefield Australian SKA Pathfinder (ASKAP) *L*-band Legacy Allsky Blind surveY (WALLABY; Koribalski et al. 2020) and the Deep Investigation of Neutral Gas Origins (Meyer 2009) survey with the ASKAP telescope (Deboer et al. 2009), and the H I component of the MeerKAT International GHz Tiered Extragalactic Exploration (MIGHTEE) survey (Jarvis et al. 2017; Maddox et al. 2021), and MIGHTEE-H I with the MeerKAT telescope (Jonas & MeerKAT Team 2016).

While many of these surveys will realistically probe out to $z \sim 0.5$, the Looking At the Distant Universe with the MeerKAT Array (LADUMA; Holwerda, Blyth & Baker 2012; Blyth et al. 2016) is set to be the deepest HI emission survey. LADUMA will use the MeerKAT *L* and *UHF* bands to probe the evolution of gas in galaxies over cosmic time, through over 3000 h on a single pointing on the sky that encompasses the Extended Chandra Deep Field South (ECDFS). The deep LADUMA pointing is predicted to probe dwarf galaxies down to HI masses ($M_{\rm H1}$) of $\sim 1 \times 10^8 \, {\rm M_{\odot}}$. This allows for direct and stacked HI emission detections up to redshifts (*z*) of $\gtrsim 1$. Moreover, ECDFS has an impressive array of ancillary data in place or forthcoming, enabling correlations with a wide range of other galaxy properties. LADUMA thus will study the redshift evolution of the BTFR through HI 21-cm observations further out than any other study.

In preparation for LADUMA, we here make predictions for the BTFR redshift evolution using the SIMBA (Davé et al. 2019) suite of cosmological hydrodynamical simulations. A local redshift study of the BTFR from galaxy rotation curves was conducted in Glowacki, Elson & Davé (2020), which found reasonable agreement with the *Spitzer* Photometry and Accurate Rotation Curves Survey (Lelli et al. 2016), albeit with some interesting discrepancies in the mass dependence of the BTFR. This study included an examination of different rotational velocity methods from galaxy rotation curves, as well as dependences of the rotation curve shape on the galaxy stellar mass and H_I gas fraction. Here, we extend this work to include spectral line width measures from mock H_I data cubes across five redshift snapshots out to z = 1, to investigate the redshift evolution of the BTFR and thus determine how viable it will be to probe this using LADUMA. Furthermore, we compare these velocity measures

This paper is organized as follows: In Section 2, we describe SIMBA and outline our sample, our method of generating HI data cubes, the observational rotational velocity measure used, and the dark matter velocity dispersion measurement. In Section 3, we compare our velocity measures from rotation curves with those from spectral line profiles, and then consider the redshift evolution in the BTFR for all galaxies in our sample, and a discy galaxy subsample. Lastly, we compare these measures to the dark matter velocity dispersion, and the dark matter halo mass. We summarize our findings in Section 5.

2 SIMULATIONS AND ANALYSIS

2.1 SIMBA

We employ the SIMBA simulation suite for this analysis (Davé et al. 2019). SIMBA is a cosmological hydrodynamic simulation evolved using the GIZMO code (Hopkins 2015), which itself is an offshoot of GADGET-3 (Springel 2005). GIZMO uses a meshless finite mass hydrodynamics solver that is shown to have advantageous features over smoothed particle hydrodynamics and Cartesian mesh codes, such as the ability to evolve equilibrium discs for many dynamical times without numerical fragmentation (Hopkins 2015), which is desirable for studying the rotation properties of galaxies. SIMBA also reproduces observations such as stellar growth (Davé et al. 2019), cold gas properties (Davé et al. 2020), and the radio galaxy population (Thomas et al. 2020).

The assumed cosmology is concordant with Planck Collaboration XIII (2016): $\Omega_{\rm M} = 0.3$, $\Omega_{\Lambda} = 0.7$, $\Omega_{\rm b} = 0.048$, $H_0 = 68$ km s⁻¹ Mpc h^{-1} , $\sigma_8 = 0.82$, and $n_s = 0.97$. In this study, we only consider the high-mass resolution ('SIMBA-hires') snapshot box. SIMBA-hires has $8 \times$ better mass resolution and $2 \times$ better spatial resolution than the fiducial 100 Mpc h^{-1} run in Davé et al. (2019), and so allows for more dwarf galaxies to be included - that is, this snapshot includes lower mass galaxies compared to the fiducial 100 Mpc h^{-1} run. SIMBAhires has a box size of 25 Mpc h^{-1} , with 512³ dark matter particles and 512^3 gas elements. This yields a mass resolution of 1.2×10^7 M_{\odot} for dark matter particles and $2.28 \times 10^6 M_{\odot}$ for gas elements. Adaptive gravitational softening length is employed with a minimum Plummer equivalent softening of $\epsilon_{\min} = 0.5 h^{-1}$ ckpc. A description of the star formation, feedback, and accretion mechanisms employed in SIMBA is provided in Glowacki et al. (2020), and in further detail in Davé et al. (2019).

We initially consider snapshots at three different redshifts: z = 0, 0.5, and 1. As in Glowacki et al. (2020), in order to select galaxies with active star formation and sufficient gas and stellar particles, we impose the following limits on galaxies within these snapshots: $M_{\rm H\,I} > 1.25 \times 10^8 \,{\rm M}_{\odot}, M_* > 7.25 \times 10^8 \,{\rm M}_{\odot}$, and $sSFR > 1 \times 10^{-11} \text{ yr}^{-1}$. These limits ensure that we only consider galaxies above the stellar mass resolution limit (i.e. are resolved) for the SIMBA-hires snapshots, and which have sufficient HI content to compare to observations and match the $M_{\rm HI}$ limit of LADUMA, and further have active star formation. This imposes a bias against lower stellar mass galaxies in this study, but unfortunately galaxies below this stellar mass resolution limit in SIMBA are poorly represented owing to too few (<32) star particles. We also visually inspect and remove galaxies undergoing obvious merger events. For our three redshift snapshots from low to high redshift, we obtain 1043, 559, and 180 galaxies.

Our sample sizes are roughly comparable to the expected numbers of galaxies to be detected in LADUMA: below redshifts of z < 0.4, 630-1300 detections are predicted [dependent on the effect of radio frequency interference (RFI)-afflicted frequencies]; between redshifts of 0.4 and 0.56, ~1200 sources; and between redshifts of 0.56 and 1.4, \sim 700 galaxies in total (based on Oxford S³ simulations; Obreschkow et al. 2009b). The field of view of LADUMA of 2 deg² at $z \sim 0.58$ (Blyth et al. 2016) corresponds to 48 Mpc, which is comparable to SIMBA-hires' box size of 25 Mpc h^{-1} (roughly 37 Mpc at each redshift) - we note that as redshift increases, the LADUMA field of view increases, owing to observing HI at lower frequencies. By not using the larger volume snapshot galaxies, we also minimize the number of massive $(M_* > 10^{10} M_{\odot})$ galaxies, which we do not expect to see large numbers of in LADUMA compared to shallower HI surveys covering a larger area, such as MIGHTEE-HI (Jarvis et al. 2017). LADUMA is also predicted to probe dwarf galaxies down to HI masses ($M_{\rm HI}$) of $\sim 1 \times 10^8 {\rm M}_{\odot}$ at low redshifts, making SIMBA-hires a good sample to use for predictions for LADUMA.

From these SIMBA galaxies, we also consider a further subsample during the analysis based on galaxy morphology. While LADUMA will detect galaxies in all morphologies in their H I emission, BTFR studies have focused on the disc galaxy population, given elliptical galaxies, which are kinematically dominated by velocity dispersion rather than rotational velocity, do not observe the same tight relation. To distinguish between discy galaxies and otherwise, we employ the κ_{rot} measure, the fraction of kinetic energy invested in ordered rotation, as described in Sales et al. (2012):

$$\kappa_{\rm rot} = \frac{K_{\rm rot}}{K} = \frac{1}{K} \sum \frac{1}{2} m \left(\frac{j_z}{r}\right)^2,\tag{1}$$

where j_z is the specific angular momentum perpendicular to the disc. In that work, they characterize simulated galaxies with $\kappa_{rot} < 0.5$ as spheroid dominated, and $\kappa_{rot} > 0.7$ as disc dominated. Therefore, we employ the same $\kappa_{rot} > 0.7$ limit to select our discy galaxies for each snapshot. Roughly 15–20 per cent of our SIMBA galaxies in each redshift sample qualify as disc dominated. We have verified that this matches our visual inspection of galaxies, and given this and the results of Sales et al. (2012), we expect that results will agree well with discy galaxies in LADUMA. We note that LADUMA will rely on multiwavelength follow-up to identify discy galaxies, and will not by itself measure κ_{rot} .

In order to better examine the BTFR for discy galaxies, we also consider discy galaxies from the snapshots at z = 0.25 and 0.75. These samples contain 136 and 53 galaxies, respectively. These galaxies underwent the same selection criteria and process as the discy z = 0, 0.5, and 1 samples.

2.2 HI spectra

We generate HI cubes via MARTINI.¹ MARTINI is a package for creating synthetic resolved HI line observations – aka data cubes – of smoothed particle hydrodynamical simulations of galaxies. It allows for realistic mock observations in that one can set the spectral resolution, cube size, and galaxy inclination relative to the observer, and convolve the beam with a radio beam and incorporate noise into the output data cube. MARTINI takes the input snapshot file and accompanying CAESAR² catalogue, a particle-based extension to

YT,³ which contains the galaxy and host halo properties including H I fraction values. MARTINI also accepts user-defined measures of the galaxy distance, rotation, and radio observation properties (spatial and spectral cube resolution, noise, and radio beam dimensions) as inputs. We note that the H I fraction in each gas particle is computed in SIMBA, accounting for self-shielding on the fly based on the prescription in Rahmati et al. (2013), and includes photoionization from a spatially uniform ionizing background given by Haardt & Madau (2012).

We opt to use properties that match the 32K mode of the MeerKAT telescope, to be employed for the upcoming LADUMA and MIGHTEE-H I surveys; that is, we use a spectral resolution of 5.51 km s^{-1} , a common radio beam of $\sim 10 \text{ arcsec}$ (BMAJ and BMIN, the major and minor axes of the radio beam, of 11.2 and 9.8 arcsec, as per early *L*-band MeerKAT observations of LADUMA), and noise values of 5×10^{-8} Jy arcsec⁻² before convolution. All galaxies were inclined such to be edge-on to the observer, so that no inclination correction is required to the rotational velocity measures.

We extract an H I spectrum from each data cube through spectralcube⁴ (PYTHON module), which has also been employed in early science and data verification analysis of LADUMA. Fig. 1 shows two spectra for a large galaxy and a small galaxy ($M_{\rm H\,I} \sim 4 \times 10^9$ and $2 \times 10^8 {\rm M}_{\odot}$) in the right-hand panels. Alongside each spectrum in the left-hand panels are each galaxy's corresponding rotation curves as constructed in Glowacki et al. (2020), based on the enclosed mass at a given radius. The larger galaxy shows a double-horned profile typical of disc galaxy rotation curves. The smaller galaxy is also identified as rotationally supported, but has a less well defined disc and shows a more Gaussian-like profile.

2.3 Rotational velocity measures

We consider the following three rotational velocity measures from the rotation curves and spectra that are used in observational studies:

(i) V_{flat} – the average circular velocity along the flat part of the rotation curve, defined in Lelli et al. (2016) as the average of outermost points of a rotation curve with relative cumulative differences smaller than 5 per cent in rotational velocity. We choose V_{flat} as this measure was found to give the tightest (least amount of scatter) BTFR than other velocity measures, both for the SPARC observational sample (Lelli et al. 2019) and SIMBA galaxies (Glowacki et al. 2020). Furthermore, we find a better agreement between the SPARC and SIMBA samples for this definition, which is less sensitive than e.g. V_{max} to an excess of dark matter content in the cores of SIMBA galaxies. To determine the maximum radius for the rotation curve, we use the HI mass-size relation to calculate the expected radius of each galaxy, at an H I mass surface density level of $1 \text{ M}_{\odot} \text{ pc}^{-2}$. There exists a tight relation between the HI mass and the extent of the HI disc for spiral galaxies in observational work (Broeils & Rhee 1997; Verheijen & Sancisi 2001; Swaters et al. 2002; Noordermeer et al. 2005; Wang et al. 2016). We apply the relation given in Wang et al. (2016) to the HI masses we have within SIMBA for each galaxy to derive an HI radius.

(ii) $W_{50}/[2\sin(i)]$ – the width at 50 per cent of a flux value, divided by 2 as per observational studies (e.g. Ponomareva et al. 2017; Lelli et al. 2019). We note that in MARTINI all cubes are rotated so that the inclination angle $i = 90^{\circ}$ for each galaxy, and so $\sin(i) = 1$.

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<sup>1</sup>https://github.com/kyleaoman/martini
<sup>2</sup>https://caesar.readthedocs.io/en/latest/
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³https://yt-project.org/

⁴https://spectral-cube.readthedocs.io/en/latest/



Figure 1. Rotation curves and H I 21-cm spectra for two example SIMBA galaxies (one massive and one dwarf galaxy, with $M_{\rm H I} \sim 4 \times 10^9$ and 2×10^8 M_☉, respectively) from the high-resolution snapshot at z = 0. The rotation curves are computed as described in Glowacki et al. (2020). H I spectra are obtained from an H I cube created through MARTINI with the spectral resolution of MeerKAT at 1420 MHz (5.51 km s⁻¹), and convolved with a standard radio beam and noise. The W_{50} and W_{20} values – the width at 50 and 20 per cent of the 90th percentile of the flux – are overplotted. The 90th percentile flux value is indicated by the grey dot–dashed line.

Therefore, we henceforth refer to this measure as $W_{50}/2$. We opt to use the 90th percentile of the highest flux measurement as opposed to the peak flux, as this results in a lower spread of values, but the main conclusions do not change based on either approach.

(iii) $W_{20}/2$ – as with $W_{50}/2$, but half the width at 20 per cent of the 90th percentile of the peak flux.

Fig. 1 (right-hand panels) shows the computation of W_{50} (vertical red dashed line) and W_{20} (vertical blue dashed line) for our two example spectra.

We also obtain, as defined in the CAESAR files of SIMBA, the dark matter halo velocity dispersion (henceforth σ_{DM}), to compare the above velocity measures with directly, and see how these observational measures serve in place of σ_{DM} in the BTFR. CAESAR uses a friends-of-friends algorithm to identify haloes, with a linking length of 0.2 times the mean interparticle spacing. We consider both dark matter particles in the host galaxy's dark matter halo, and only dark matter particles within the radius from the galaxy's centre of mass used as the cut-off distance for the galaxy's rotation curve (ergo, determined by the H I mass–size relation, using the $M_{\rm H1}$ from CAESAR and the relation found in Wang et al. 2016, as done for the rotation curves in Glowacki et al. 2020), which is typically much smaller than

the virial radius. Unless mentioned otherwise, we typically consider the $\sigma_{\rm DM}$ from the whole galaxy dark matter halo.

3 RESULTS

3.1 Rotational velocity comparisons

Before we consider the redshift evolution in the BTFR, we want to compare our spectral line width measures, $W_{50}/2$ and $W_{20}/2$, with the V_{flat} measure from rotation curves. We do not expect a perfect correlation between these different measures. W_{50} and W_{20} measure different parts of the H_I spectrum and so, as the spectrum shape changes from the classic double-peaked shape for massive galaxies to single-peaked shapes (see examples in Fig. 1), the difference between W_{50} and W_{20} also evolves. However, any deviation identified may inform us on where other relations can break down for our simulated galaxy sample.

In Fig. 2, we plot the spectral width measurements against V_{flat} for the redshift z = 0 snapshot. $W_{50}/2$ occupies the left-hand panels, and $W_{20}/2$ the right. The top panels are for the full sample, and bottom panels are for the discy subsample. Points are coloured by the stellar mass, and the 1:1 relation is given by the black dashed lines.



Figure 2. W_{50} (left) and W_{20} (right) versus V_{flat} , coloured by galaxy stellar mass, for SIMBA galaxies. The top panels are for the full sample, and bottom panels are for discy galaxies. The 1:1 relation is given in the black dashed lines.

Considering the full sample first, $W_{50}/2$ follows the 1:1 relation at higher masses ($M_* > 10^{9.5} M_{\odot}$), but at lower masses in the full sample (or alternatively below rotational velocities of ~100 km s⁻¹) $W_{50}/2$ gives lower rotational velocities than V_{flat} . While this effect is also present for $W_{20}/2$, it is far less pronounced. It is possible that it is because the $W_{20}/2$ measure, made at a lower section of the spectrum, is less sensitive to changes in the spectrum shape than width measures made closer to the peak flux, as $W_{50}/2$ is. We also find a lower scatter from $W_{20}/2$ than for $W_{50}/2$, which holds true throughout this study when either are used to compare different relations.

We rule out that the higher V_{flat} measures at low masses in the full sample are driven by the rotation curve shape; unlike in observational studies, the rotation curves for our low-mass SIMBA galaxies still exhibit a peak and flattening in their shape, rather than continually rising, which is an issue with SIMBA that was noted in Glowacki et al. (2020). This may be simply because we are not affected in sensitivity with simulated galaxies to reach the H I mass–size relation distance used to determine the extent of the rotation curve, which may be an issue for observational studies for lower mass galaxies.

To verify this, we fitted the Polyex parametric model (Giovanelli & Haynes 2002) to all rotation curves in our sample here (see fig. 4 of Glowacki et al. 2020). The Polyex parametric model V_{polyex} is defined as

$$V(r) = V_0 (1 - e^{-r/r_{\rm pe}})(1 - \alpha r/r_{\rm pe}),$$
⁽²⁾

where V_0 regulates the overall amplitude of the rotation curve, r_{pe} is the scale length for the inner steep rise of the rotation curve, and yields a scale length for the inner steep rise, and α sets the slope of the slowly varying outer part. No trend was found with stellar mass between the r_{pe} parameter of Polyex with the radius at which the maximum velocity of the rotation curve occurs, normalized by the extent of the rotation curve's radius. Therefore, there is no evidence that the higher peak in SIMBA galaxy rotation curves, which corresponds to the radius at which the peak V_0 occurs in Polyex, is caused by the rotation curve shape itself. Furthermore, the same downturn between spectral line width and V_{flat} is seen for other velocity measures from the rotation curve, e.g. V_{max} .

Redshift evolution of the BTFR in SIMBA

The discy sample (bottom panels) better follows the 1:1 relation and lacks the downturn at low $V_{\rm flat}$ values, particularly for the smaller galaxies. This indicates that the line widths fail to trace $V_{\rm flat}$ in lowmass, dispersion-dominated galaxies, which is perhaps unsurprising because the majority of those are not discy. Instead, low-mass SIMBA galaxies are more supported by dispersion than by rotation, as seen in elliptical and irregular galaxies. Therefore, for lower mass galaxies in the full sample we can potentially expect to see some deviation from any trend found for the BTFR or with $\sigma_{\rm DM}$.

Fitting a line with unity slope to the discy sample, we get an amplitude offset of about 0.05 dex for the W_{50} measure and 0.2 dex for W_{20} relative to V_{flat} . This shows that W_{50} nicely traces V_{flat} as expected, while W_{20} does also albeit with a small offset. None the less,



Figure 3. The redshift evolution of the BTFR for V_{flat} , σ_{DM} , $W_{50}/2$, and $W_{20}/2$, for all galaxies selected from each snapshot (not specifically just discy galaxies). A simple linear fit is given in dashed lines; we note that the relation steepens for V_{flat} at lower baryonic masses. Visually, the distributions are distinct for the top two panels, but harder to separate when using spectral line widths due to contamination of non-disc galaxies. The $W_{50}/2$ measure has a significant scatter.

 W_{20} provides a tighter relation versus V_{flat} (orthogonal intrinsic scatter of $\sigma_{\perp} = 0.039$ for W_{20} versus $\sigma_{\perp} = 0.057$ for W_{50} ; see Section 3.2.1 for further details on σ_{\perp} measurements). Thus, both these measures are useful for tracing the rotation velocities of galaxies in lieu of resolved data.

Overall, for SIMBA galaxies we see good agreement between our rotational velocity measures from spectral line widths and rotation curves, albeit with a fixed offset. Next, we consider how each of these measures, alongside σ_{DM} , compares with the BTFR at different redshifts.

3.2 Redshift evolution of the BTFR

Armed with our various rotation measures, we can now examine the redshift evolution of the BTFR. We now also include σ_{DM} as a rotation measure, in order to understand how well this quantity is traced by H_I-based galaxy rotation measures. All plots on the BTFR use M_{bar} , the baryonic mass of each galaxy (i.e. the cool, dense gas plus stellar mass). By redshift evolution, we refer to both the slope and y-intercept (or normalization) of the BTFR.

3.2.1 H1-rich star-forming galaxies

We begin in Fig. 3, by considering the full sample selected to have significant H I, as described in Section 2.1. While this sample includes some non-discy galaxies, this is the sample that represents what will be directly identified from LADUMA. Discy galaxies from LADUMA will need to be identified with ancillary data, and so we wish to first consider the larger SIMBA sample in order to highlight the importance for LADUMA to identify spiral galaxies. We plot the

BTFR for each rotational velocity measure and σ_{DM} in each panel, on a log–log plot. Redshift z = 0 results are given in blue, z = 0.5in green, and z = 1 in red. Also shown are the best-fitting linear relations, in matched colours.

Table 1 gives the values and 1σ errors for the best-fitting linear values for slope m, y-intercept b, and their orthogonal intrinsic scatter σ_{\perp} . The measure of scatter is quantified as in Lelli et al. (2019) and Glowacki et al. (2020) through the standard affine-invariant ensemble sampler in EMCEE (Foreman-Mackey et al. 2013), which includes inverse variance weighting. The best-fitting relation from the $\sigma_{\rm DM}$ measure at z = 0 is given in each panel for comparison, as the black dashed line. We note that at times in our efforts to simulate the LADUMA survey through this sample, the sample size is limited, especially for the discy subsample (see the second half of Table 1). Therefore, in estimating the errors, we both use 100 random walkers through the EMCEE fitting routine, and repeat on 50 sets of bootstrapping (random sampling with replacement) to obtain realistic error estimates. Errors quoted for the slope, y-intercept, and scatter are taken from the standard deviation of our bootstrapping results. Our measured median values for these parameters do not change significantly between the bootstrapping approach and a single EMCEE analysis of the original set.

In regard to scatter, for all redshifts we see that $W_{50}/2$ has the largest spread, which is also evident visually, particularly at the low baryonic mass or velocity end. This likely also contributes to the significantly flatter BTFR slopes we see for this measure. The results for $W_{50}/2$ are attributed to low velocity values, which may be due to the inclusion of non-discy galaxies. Another effect could be the discrete spectral resolution of the H I data cube. As shown in Fig. 1, $W_{50}/2$ will be smaller than $W_{20}/2$, and so the effect is lessened for $W_{20}/2$ for galaxies with low baryonic mass.

Table 1. The best-fitting BTFRs for different rotational velocity definitions: V_{flat} from rotation curves, $W_{50}/2$ and $W_{20}/2$ from spectral line widths, and the dark matter velocity dispersion (σ_{DM}), for different redshift snapshots. We give the slope (m), y-intercept (b), and the orthogonal intrinsic scatter (σ_{\perp}) in dex for $\log_{10} (M_{\text{bar}}) = m \log_{10} (V) + b$. The standard deviation from 50 sets of bootstrapping on each sample is given as an error for each parameter. We compare between the full sample (which requires a minimum HI mass, stellar mass, and sSFR) and a discy subsample that additionally requires $\kappa_{\text{rot}} > 0.7$, at different redshifts.

Velocity definition	Redshift	Sample size	m	b	σ_{\perp}
Full sample					
V _{flat}	0	1043	4.38 ± 0.07	0.56 ± 0.13	0.070 ± 0.004
V _{flat}	0.5	559	3.67 ± 0.14	$2.34~\pm~0.28$	$0.078~\pm~0.011$
V_{flat}	1	180	3.64 ± 0.12	2.60 ± 0.25	0.075 ± 0.014
$\sigma_{ m DM}$	0	1043	3.54 ± 0.09	2.55 ± 0.17	0.073 ± 0.007
$\sigma_{ m DM}$	0.5	559	$2.85~\pm~0.08$	3.96 ± 0.16	0.101 ± 0.014
$\sigma_{ m DM}$	1	180	3.22 ± 0.08	3.06 ± 0.16	0.066 ± 0.008
W ₅₀ /2	0	1043	2.60 ± 0.04	$4.32~\pm~0.08$	0.115 ± 0.008
$W_{50}/2$	0.5	559	$2.27~\pm~0.08$	5.17 ± 0.15	0.143 ± 0.019
$W_{50}/2$	1	180	2.20 ± 0.12	5.41 ± 0.25	0.159 ± 0.027
W ₂₀ /2	0	1043	3.50 ± 0.04	$2.22~\pm~0.08$	0.068 ± 0.004
$W_{20}/2$	0.5	559	$2.64~\pm~0.12$	3.97 ± 0.24	0.090 ± 0.019
W ₂₀ /2	1	180	$2.97~\pm~0.08$	3.40 ± 0.17	0.092 ± 0.011
Discy galaxy subsample ($\kappa_{\rm rot} > 0.7$)					
V _{flat}	0	204	3.62 ± 0.12	$2.42~\pm~0.25$	0.086 ± 0.013
V _{flat}	0.25	136	3.33 ± 0.09	3.17 ± 0.18	0.094 ± 0.010
V _{flat}	0.5	86	3.91 ± 0.22	$1.93~\pm~0.46$	0.073 ± 0.017
V _{flat}	0.75	51	3.78 ± 0.24	2.29 ± 0.51	0.056 ± 0.004
V_{flat}	1	33	$4.43~\pm~0.38$	0.94 ± 0.81	0.047 ± 0.025
$\sigma_{\rm DM}$	0	204	3.27 ± 0.06	$3.27~\pm~0.12$	0.078 ± 0.007
$\sigma_{\rm DM}$	0.25	136	2.78 ± 0.09	4.27 ± 0.19	0.104 ± 0.015
$\sigma_{\rm DM}$	0.5	86	2.86 ± 0.12	3.95 ± 0.26	0.120 ± 0.027
$\sigma_{\rm DM}$	0.75	51	3.01 ± 0.14	3.56 ± 0.32	0.056 ± 0.007
$\sigma_{ m DM}$	1	33	3.27 ± 0.18	2.92 ± 0.40	0.061 ± 0.016
W ₅₀ /2	0	204	3.02 ± 0.15	3.52 ± 0.31	0.111 ± 0.028
$W_{50}/2$	0.25	136	2.67 ± 0.31	4.21 ± 0.48	0.148 ± 0.056
$W_{50}/2$	0.5	86	2.36 ± 0.21	4.88 ± 0.47	0.162 ± 0.074
$W_{50}/2$	0.75	51	4.83 ± 0.48	-0.62 ± 1.10	0.093 ± 0.060
$W_{50}/2$	1	33	5.02 ± 0.59	-1.21 ± 1.36	0.065 ± 0.086
W ₂₀ /2	0	204	$4.06~\pm~0.10$	$1.07~\pm~0.23$	0.057 ± 0.007
$W_{20}/2$	0.25	136	3.92 ± 0.17	1.32 ± 0.32	0.070 ± 0.017
$W_{20}/2$	0.5	86	$4.02~\pm~0.18$	0.99 ± 0.39	0.073 ± 0.011
$W_{20}/2$	0.75	51	4.28 ± 0.25	0.33 ± 0.42	0.048 ± 0.017
$W_{20}/2$	1	33	5.09 ± 0.27	-1.65 ± 0.59	0.051 ± 0.018

The other two observational measures, and the non-observational method $\sigma_{\rm DM}$, have similar values of scatter as each other. This suggests that for better results in LADUMA, velocity measure that traces a wider width from the H I spectral line profile is recommended at higher redshift, and for local galaxy measures from rotation curves. We note that in Lelli et al. (2019) they use $W_{\rm M50}$, the line width at 50 per cent of the mean flux density, rather than the peak, ergo a value comparable to W_{20} , and found similar measures of scatter for $W_{20}/2$ and $W_{\rm M50}/2$ for SPARC galaxies.

As mentioned, this full sample does not contain only discy galaxies, but also includes dispersion-dominated galaxies. We thus do not focus on analysis for this sample, beyond making the observation that the large scatter prevents a clear redshift evolution of the BTFR to be apparent through the spectral line width measures. As galaxies at higher redshift will not be spatially resolved by MeerKAT, measures from rotation curves such as V_{flat} will not prove a practical method. This means that spectral line widths must be relied upon in a redshift evolution study. As shown here, these measures are not ideal for

tracing V_{flat} based on the full sample from SIMBA – therefore, LADUMA must be able to distinguish between discy and elliptical morphologies. Happily, this is not the end of the tale.

3.2.2 Discy galaxies

The sample considered earlier was merely star-forming galaxies with sufficient H I gas, not just discy galaxies, which is what the BTFR focuses on. While LADUMA will detect H I emission in galaxies of all morphologies, it will be able to discern between host galaxy morphologies only due to the wealth of multiwavelength data available in the ECDF-S (Holwerda et al. 2012). Hence, in Fig. 4 we consider the subsample of SIMBA galaxies with discy morphologies, using the $\kappa_{rot} > 0.7$ limit. Their best fits are also included in Table 1. We note that the same trend in scatter is seen for the discy subsample as in the full sample. We include the discy galaxies in the z = 0.25 and 0.75 snapshots in this analysis, so as to better examine the trend within redshifts 0–1.



Figure 4. As in Fig. 3, but with a cut for discy ($\kappa_{rot} > 0.7$) galaxies, and including galaxies at z = 0.25 and 0.75. The redshift evolution is more pronounced in the $W_{20}/2$ measure for these discy galaxies. The scatter in $W_{50}/2$ is too large for convincing redshift evolution to be seen. The improvement in these relations compared to Fig. 3 showcases the importance of galaxy morphological identification in LADUMA.

First, we consider $\sigma_{\rm DM}$, which the BTFR aims to trace through observational methods. The z = 0.5 galaxies have a flatter slope than for redshift z = 0, while the slope for z = 1 is within 1σ of the bestfitting slope of the z = 0 sample. The *y*-intercept meanwhile grows between $z = 0 \rightarrow 0.5$, but drops again to z = 1. Visually, we see that the higher redshift galaxies tend to occupy the lower right-hand side of the plot. To better quantify this, in Fig. 5 we give the baryonic mass for the best-fitting relation at fixed velocities of 100 and 200 km s⁻¹. For $\sigma_{\rm DM}$ (black points), the baryonic mass decreases with increasing redshift (or alternatively, at fixed baryonic mass, galaxies rotate faster at higher redshift).

Curiously, we see that the visual redshift evolution trends are reversed for V_{flat} ; when using σ_{DM} , the higher redshift galaxies have larger dark matter velocity dispersions than at lower redshift, while with V_{flat} it is the lower redshift galaxies with higher rotational velocities. Quantitatively, V_{flat} has an increase in baryonic mass at fixed velocity with redshift, albeit this is weak between z = 0and 1 at lower fixed velocities; the trend is more convincing (> 3σ significance) at $V = 200 \text{ km s}^{-1}$ (red points of Fig. 5). As this 'reversed' trend is not seen for the spectral line widths (see below), it is possible that there is a redshift evolution between V_{flat} and σ_{DM} that does not occur for the spectral line widths with σ_{DM} . We investigate this in Section 3.3. We also note that, as in the simulated galaxy samples in Brook, Santos-Santos & Stinson (2016) and Sales et al. (2017), there is a turn-off in the BTFR at the lower mass or rotational velocity end ($V < 100 \text{ km s}^{-1}$) for our simulated SIMBA galaxies for V_{flat} , which hence affects the BTFR linear fits on which the trends in Fig. 5 rely upon.

Considering the spectral line width measures now, $W_{20}/2$ has the same general trend as σ_{DM} in Fig. 5, with the higher redshift

disc galaxies having a lower baryonic mass at fixed velocity (3σ significance) than the lower redshift disc galaxies. This is once again opposite to the distribution seen visually for V_{flat} , although all observational measures show a steepening in the slope between redshift 0 and 1 (second half of Table 1). While the scatter remains largest for $W_{50}/2$, and there is no clear redshift trend in the bottom panel of Fig. 5 (green points), at 100 km s⁻¹ the corresponding baryonic mass from the best-fitting relations follows the same trend as for $\sigma_{\rm DM}$ and W_{20} . W_{50} also visually agrees with that of $W_{20}/2$ and $\sigma_{\rm DM}$ in that higher redshift sources lie on the lower right of the BTFR plot. Quantitatively, both the slope and y-intercept at z= 1 for W_{20} differ from the lower redshift samples by over 3σ , and this is also seen for $W_{50}/2$. We note that source numbers are lower for this discy subsample (Table 1), but that these numbers are again comparable to the expected number from the LADUMA survey.

The above analysis depends on the best BTFR fits made to each of these relations, and for many there is no clear trend in slope or intercept with redshift for each sample from one redshift sample to another, within the total redshift range of 0–1. As described in the following subsection, studies such as Übler et al. (2017) suggest that the zero-point, or *y*-intercept, of the BTFR changes between redshifts z = 0 and 0.9. To see whether this trend exists for our simulated LADUMA sample, in Fig. 6 we repeat our BTFR fits but fix the slope in each case to the slope found in the redshift z = 0 case (Table 1). For $\sigma_{\rm DM}$ and the spectral line widths, we see a decrease in the *y*-intercept of these best-fitting relations with increasing redshift, which again is seen to an $\sim 3\sigma$ significance. The trend is once again reversed for $V_{\rm flat}$. While we stress that the effect is weak, especially for instance between redshifts z = 0 and 0.75 in the case of W_{20} , there



Figure 5. The baryonic mass $M_{\rm bar}$ for the best-fitting relations for discy galaxies (Fig. 4) versus redshift, at rotational velocities of 100 km s⁻¹ (top panel) and 200 km s⁻¹ (bottom panel). At both velocities, $\sigma_{\rm DM}$ and W_{20} decrease in $M_{\rm bar}$ with redshift, while $V_{\rm flat}$ increases.

is evidence of redshift evolution in the *y*-intercept for this simulated LADUMA sample when the slope is fixed.

We hence conclude that LADUMA will be able to study and detect a weak redshift evolution of the BTFR through the use of spectral line widths. Such a study will be better suited to using $W_{20}/2$ rather than $W_{50}/2$, and will benefit from focusing on discy galaxies identified through auxiliary data to best observe this effect. As LADUMA will already be relying on additional, non-radio data available to e.g. obtain stellar masses necessary for this study, this is encouraging news.

There are a couple of caveats to this. For one, while our SIMBA HI data cubes are already convolved with a radio beam and with noise included in the spectrum, all galaxies were rotated so that no inclination correction was required. This correction effect and potential difficulty in obtaining accurate inclination measures for high-redshift targets, assumptions in the stellar mass-to-light ratio used for the baryonic mass measure, and any additional observing factors such as RFI, will introduce errors into the study to be undertaken in the LADUMA survey. Lastly, there remains discrepancies between SIMBA-simulated galaxies and true galaxies, such as an excess amount of dark matter in the core of SIMBA galaxies (Glowacki et al. 2020). None the less, we expect that such factors will not prevent the successful study of the HI redshift evolution of the BTFR in LADUMA.

3.2.3 Comparison with previous studies

We briefly compare our findings with other simulated and observational studies mentioned in the introduction. We note, as summarized in Abril-Melgarejo et al. (2021), that the evolution of the TFR with cosmic time has remained a matter of debate, and that many different methods (e.g. integral field spectroscopy) to study the TFR have been used, as opposed to HI observations from radio telescopes that we simulate here.

Portinari & Sommer-Larsen (2007) used an improved version of 'SGP03' simulations (Sommer-Larsen, Götz & Portinari 2003), and found negligible redshift evolution between redshifts (z) of 0 and 1 in the *stellar* TFR, although their sample only included ~25 disc galaxies. Their findings with simulated galaxies for the stellar TFR agree with various observational studies, such as Tiley et al. (2019) between z = 0 and 1. However, redshift evolution of the zero-point (i.e. the *y*-intercept) of the stellar TFR was found in Puech et al. (2008) between redshifts (z) of 0 and 0.6, and Übler et al. (2017) found the same for redshifts between 0 and 0.9, although not between redshifts of 0.9 and 2.3. Barden et al. (2003), through near-infrared H α observations of $z \approx 1$ disc galaxies, found a brightening by 1.1 mag in the rest-frame *B*-band TFR compared to local galaxies, while Bamford, Aragón-Salamanca & Milvang-Jensen (2006) saw a brightening of 1.0 mag between z = 0 and 1 spiral galaxies.

We highlight that the inclusion of the HI mass, as well as the approach in measuring the TFR using HI line widths, is an important difference between our work on the BTFR and studies focusing on the stellar TFR. One example of this is that low-mass systems are completely HI dominated in terms of baryonic content. None the less, the trend Puech et al. (2008) and Übler et al. (2017) observe in the stellar TFR agrees with what we find in Fig. 4 for the BTFR: At comparable stellar or baryonic masses, higher redshift galaxies rotate faster. This can be explained through the virial theorem – since $M \propto RV^2$, then for a higher redshift galaxy with the same mass *M* and smaller radius *R* than a local galaxy, the velocity *V* of the higher redshift galaxy must hence increase. In SIMBA, as in observations, the size of star-forming galaxies decreases to higher redshifts (Appleby et al. 2019), thereby driving a higher rotational velocity.

Obreschkow et al. (2009a) consider the BTFR through the Millennium Simulation for 3×10^7 galaxies of various morphologies, albeit at a far broader range of redshifts (z = 0, 4.89, and 10.07). They use the W_{20} measure of the H I content and find that galaxies of identical baryonic mass have broader H I profiles, and hence larger circular velocities, at higher redshift, a conclusion we find agreement with for SIMBA galaxies. Übler et al. (2017) also find a change in the zero-point BTFR between observed galaxies at z = 0 and 0.9, which compares well to our finding with σ_{DM} , and to a lesser extent with $W_{20}/2$, where we had fixed the slope (Fig. 6).

Conversely, Puech et al. (2010) did not see an evolution in either slope or zero-point/y-intercept in the BTFR through VLT (Very Large Telescope) observations between redshifts of 0.0 and 0.6. This roughly matches our finding for spiral galaxies between redshifts of 0.0–0.5 through $W_{20}/2$, where the slope and y-intercept best-fitting parameters agree within 1σ . It may hence mean that the LADUMA study of the redshift evolution of the BTFR will only become significantly apparent at higher redshifts, i.e. $z \sim 1$.

Obreschkow et al. (2009a) also noted that the scatter of their relation increases with redshift, which they attribute to a lower degree of virialization at higher redshifts in their model. The increased scatter was also found in the observational study of Puech et al. (2010), who attributed this to major merger events for their higher



Figure 6. As in Fig. 4, but where the slope for each best-fitting relation is fixed to the z = 0 case for all redshift samples. The best-fitting y-intercept slightly decreases with redshift for σ_{DM} and the spectral line width measures, while it increases in the case of V_{flat} .

redshift sample. We see the same effect in increasing scatter for both $W_{50}/2$ and $W_{20}/2$ in the full sample with increasing redshift, noting, however, here that we have lower sample sizes and a much smaller redshift range than the sample of Obreschkow et al. (2009a), and hence observe this trend at low significance. While we see an increase in scatter for σ_{DM} between redshifts of 0 and 0.5, the scatter decreases for the redshift z = 1 galaxies – possibly an effect of lower sample size, or perhaps a lower fraction of major mergers for these galaxies than in lower redshift snapshots here, despite our efforts to remove merging or interacting galaxies from our samples through visual inspection.

3.3 Rotational velocity with σ_{DM}

As introduced before, we also wish to consider how well do the three observational measures for rotational velocity compare with a key attribute of galaxies that *cannot* be measured from observational studies, the velocity dispersion of the dark matter particles associated with the host galaxy (σ_{DM}). As this information is available within SIMBA, we can investigate this directly, both for the full sample, when considering the discy subsample, and at different redshifts. Given that the observational velocity measures have been used with great success in studying the various forms of the TFR in the literature, and show general agreement in this study, we expect observational measures to correlate with σ_{DM} . However, as the dark matter halo properties were found to change with redshift in SIMBA galaxies, as demonstrated in Davé et al. (2019), it is important to investigate whether these correlations evolve with redshift, as this

This is also important to consider for mass modelling of galaxies, which will be done for LADUMA and could be studied as a function of redshift. In the nine-panel plot given in Fig. 7, we compare the \log_{10} rotational velocity measures with the logarithm of $\sigma_{\rm DM}$ from the

could affect our interpretation of the BTFR redshift evolution results,

such as the reverse trend seen for V_{flat} compared to other measures.

rotational velocity measures with the logarithm of $\sigma_{\rm DM}$ from the associated dark matter halo [i.e. $\log_{10} (V)$ versus $\log_{10} (\sigma_{\rm DM})$]. The left column gives $V_{\rm flat}$, the middle column $W_{50}/2$, and the right column $W_{20}/2$. The first row focuses on z = 0 galaxies, comparing the full sample (blue) with the discy subsample (green). The middle row considers the full sample at each redshift bin: Blue circles indicate z = 0 galaxies, green squares for z = 0.5, and red diamonds for z = 1. The bottom row repeats this, but gives the redshift evolution of the $V-\sigma_{\rm DM}$ relation for only discy galaxies. The 1:1 line is given in the black dashed line for reference. The best linear fit parameters and scatter measure are given in Table 2 for each measure and redshift, separated into the full sample and discy galaxy subsample. We note that we consider both the change in slope and normalization (*y*-intercept) of the relations in regard to redshift evolution in the following analysis.

First, we compare how each observational rotation measure compares in tracing σ_{DM} . At all redshifts, V_{flat} gives the tightest correlation (least scatter) with σ_{DM} . The smaller scatter may be attributed to the fact the rotation curves, which *V* is measured from, consider the distribution of all particles in a SIMBA galaxy and its halo, while spectral line widths only come from the HI gas particle information. As the HI content can be pressure supported, these measures can give different results for slow-rotating galaxies at the



Figure 7. A comparison of $\log_{10}(V)$ versus $\log_{10}(\sigma_{DM})$. For $\log_{10}(V)$, we test the rotational velocity of SIMBA galaxies calculated from rotation curves through V_{flat} (left-hand panels), and from the H I spectrum line profiles ($W_{50}/2$ and $W_{20}/2$, middle and right-hands panels, respectively). These are plotted against the dark matter velocity dispersion (σ_{DM}) from the SIMBA snapshot properties as calculated in CAESAR. The 1:1 trend is given in the black dashed line for scale. Top row: At redshift z = 0, we consider the full sample from SIMBA-hires in blue circles, and the 'discy' galaxy subsample ($\kappa_{rot} > 0.7$) in green squares, which tends to pick faster rotating galaxies. Of the three measures here, V_{flat} gives the tightest correlation, while $W_{50}/2$ is closest to the 1:1 line but has larger scatter, particularly for lower mass galaxies. Middle row: We show the redshift evolution for the full sample. Blue circles indicate z = 0 galaxies, green squares for z = 0.5, and red diamonds for z = 1. Bottom row: The redshift evolution for only discy galaxies. In both samples, redshift evolution is only seen from the V_{flat} measure.

bottom end of the BTFR. $W_{20}/2$ unsurprisingly once again performs better than $W_{50}/2$ in regard to scatter – but we note that for the full sample $W_{50}/2$ best matches the 1:1 relation. Therefore, $W_{20}/2$ may be better suited for only discy galaxies when comparing it with $\sigma_{\rm DM}$.

In the full sample at redshift z = 0, V_{flat} gives the flattest slope and highest y-intercept, by over 5σ , compared to the spectral line measures. The spectral line width measures give a steeper, close-tounity slope. However, in the discy subsample the $V-\sigma_{\rm DM}$ best-fitting slopes (values around 0.75) and y-intercepts found from all observation methods agree within 1σ at identical redshifts. Therefore, each observational method correlates with the dark matter velocity dispersion in the same manner for rotation-dominated galaxies. As $V_{\rm flat}$ is only usable to low redshift due to spatial resolution

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Table 2. Best log–log fits between the three rotational velocity measures and the dark matter velocity dispersion (σ_{DM}), as in Table 1 (see Fig. 7). Values for the different redshift snapshots and the full sample or discy subsample are given. The discy subsample has similar values to the full sample when using V_{flat} . The largest scatter is typically seen for the $W_{50}/2$ measure.

Velocity definition	Redshift	Sample size	т	b	σ_{\perp}
Full sample					
V _{flat}	0	1043	0.68 ± 0.01	$0.70~\pm~0.02$	0.039 ± 0.001
V _{flat}	0.5	559	0.63 ± 0.02	0.71 ± 0.03	$0.044~\pm~0.001$
V _{flat}	1	180	$0.77~\pm~0.04$	$0.38~\pm~0.08$	0.036 ± 0.005
W ₅₀ /2	0	1043	0.97 ± 0.03	0.06 ± 0.05	0.073 ± 0.003
$W_{50}/2$	0.5	559	0.88 ± 0.03	0.19 ± 0.06	$0.084~\pm~0.006$
$W_{50}/2$	1	180	$0.97~\pm~0.05$	-0.03 ± 0.10	0.088 ± 0.011
W ₂₀ /2	0	1043	0.90 ± 0.02	0.30 ± 0.03	0.059 ± 0.002
$W_{20}/2$	0.5	559	0.82 ± 0.03	0.44 ± 0.06	0.059 ± 0.002
$W_{20}/2$	1	180	0.90 ± 0.03	$0.26~\pm~0.07$	0.061 ± 0.003
Discy galaxy subsample ($\kappa_{\rm rot} > 0.7$)					
V _{flat}	0	204	0.76 ± 0.02	0.55 ± 0.03	0.049 ± 0.002
V _{flat}	0.5	86	0.67 ± 0.03	0.65 ± 0.06	$0.057~\pm~0.005$
V_{flat}	1	34	$0.73~\pm~0.05$	$0.48~\pm~0.10$	0.041 ± 0.007
W ₅₀ /2	0	204	0.76 ± 0.03	0.58 ± 0.06	0.073 ± 0.002
$W_{50}/2$	0.5	86	0.66 ± 0.04	0.75 ± 0.09	0.103 ± 0.009
W ₅₀ /2	1	34	0.82 ± 0.05	$0.42~\pm~0.10$	$0.047\ \pm\ 0.005$
W ₂₀ /2	0	204	0.74 ± 0.03	0.68 ± 0.05	0.052 ± 0.002
$W_{20}/2$	0.5	86	0.74 ± 0.04	0.65 ± 0.08	0.063 ± 0.005
$W_{20}/2$	1	34	0.80 ± 0.03	$0.55~\pm~0.06$	0.044 ± 0.003

requirements, the spectral line width measures would be more useful for LADUMA in this instance.

Next, we focus on the differences seen between the discy and full populations. Relative to the full sample, discy galaxies have higher $\sigma_{\rm DM}$ measures, and also higher rotational velocities. Quantitatively, the differences between the samples are more evident when using spectral line widths. The best-fitting slopes for the discy subsample and the full sample at all redshifts for $V_{\rm flat}$ agree within 2σ , as do their intercepts (sometimes within 1σ). This is not the case for the spectral line widths (top row of Fig. 7) – discy galaxies have flatter slopes and correspondingly higher *y*-intercepts than the full sample. Therefore, spectral line widths better trace the effect of galaxy morphology in its correlation with $\sigma_{\rm DM}$ from the full dark matter halo, than velocity measures from galaxy rotation curves.

We now consider the redshift evolution of the $V_{\rm obs}$ - $\sigma_{\rm DM}$ relation. At higher redshifts, galaxies have a lower rotational velocity at fixed $\sigma_{\rm DM}$. This redshift evolution is diminished for the discy subsample, and despite persisting for V_{flat} is essentially negligible when considering spectral line width measures. Redshift evolution of this relation for the full sample, which includes dispersion-dominated galaxies, might be attributed to a different merger history compared to the discy galaxies - that is, at higher redshifts, dispersion-dominated galaxies rotate slower than they do now, while this is not so apparent when considering spiral galaxies. Alternatively, at fixed rotational velocities, there is a lower dark matter velocity dispersion, which is tied to a smaller dark matter halo mass - so at higher redshift galaxies have a smaller dark matter halo, which is more apparent for dispersion-dominated galaxies. However, in Section 3.5, we note little to no redshift evolution between V_{obs} and dark matter halo mass.

When considering the full sample quantitatively, the slope does not change between redshift 0 and 1 beyond a 2σ - 3σ level. Meanwhile, the *y*-intercept *b* changes more significantly (over 3σ) for V_{flat} with redshift. The *y*-intercept does not significantly evolve with redshift

when probed by spectral line width measures, beyond being slightly higher at z = 0.5 by 2σ .

For discy galaxies, there is only an evolution of V_{flat} at fixed σ_{DM} with redshift (higher rotational velocity at lower redshift) – not for the spectral line widths. This can explain the 'reverse trend' we see in Fig. 5, where at fixed velocity the baryonic mass for σ_{DM} and W_{20} decreases with increasing redshift, but increases for V_{flat} . The lack of redshift evolution of W_{20} with σ_{DM} , meanwhile, suggests that there is no additional complication in using W_{20} for LADUMA in studying the redshift evolution of the BTFR.

We remind the reader that the dark matter velocity dispersion measurements come from the dark matter halo that the host galaxy is associated with. This hence means that the gas content traced by spectral line widths will not completely correlate with the attributes of the dark matter halo. What if we consider the dark matter particles within the baryonic extent of the galaxy, rather than the full galaxy halo?

3.4 Velocity dispersion of dark matter within the baryonic extent

It will be important to investigate whether there is a distinct difference between observational velocity and the dispersion measure for dark matter within the same extent as the baryonic matter, and the dispersion measure for the full dark matter halo. For example, with mass modelling of galaxies, the dark matter content and distribution are vital to model properly at all distances from the centre, including at inner radii. Furthermore, we can investigate whether there will be any redshift evolution of the dark matter content in the inner parts of galaxies, which can inform us on galaxy morphological evolution with redshift.

We repeat the same panel scheme as before in Fig. 8, but this time give the dark matter velocity dispersion for particles occupying the same radius from the galaxy centre of mass determined by the



Figure 8. As in Fig. 7, but using the dark matter velocity dispersion calculated from particles within a radius from the galaxy centre determined by the H I mass-size relation – therefore, lower dispersion values are seen. Redshift evolution is also stronger here, and the correlation slightly tighter at z = 0 and 0.5, but the relation shifts from the 1:1 line.

H I mass–size relation, using that found observationally in Wang et al. (2016). This is the same radius we used as the extent for the galaxy rotation curves generated to obtain the V_{flat} measure. The key difference between this and Fig. 7 is that now we only consider the dark matter content within the same extent that would be traced observationally in LADUMA (i.e. the same region as the H I gas), not the content of the entire dark matter halo of the galaxy.

In Fig. 9, we show that for most galaxies the radius we extend to in Fig. 8 ($R_{\rm H\,I}$) is less than 1/10th of R_{200} , which corresponds to the radius enclosing the total halo mass for SIMBA galaxies, irrespective of total galaxy halo mass $M_{\rm halo}$. Table 3 gives the best-fitting parameters for the relation explored in Fig. 8, henceforth $V-\sigma_{\rm DM-H\,I}$.

Many of the same findings from Fig. 7 and Table 2 still hold; namely that $V_{\text{flat}}-\sigma_{\text{DM-H1}}$ gives the tightest relation and $W_{50}/2$ the least, and that the spectral line widths trace different values of σ_{DM} for discy galaxies compared to other morphologies. However, there are a few differences – for instance, for the full sample at all redshifts, the spectral line widths give a slope much better matching a value of unity in $V-\sigma_{\text{DM-H1}}$. This shows a stronger correlation between these measures, to be expected when they consider the same volume. Likewise, the scatter is generally slightly smaller when considering $\sigma_{\text{DM-H1}}$.

One obvious new effect when comparing $V-\sigma_{\rm DM}$ with $V-\sigma_{\rm DM-H1}$ is that in the latter measure, all points shift away (towards the upper left



Figure 9. The ratio of the H_I radius (R_{H_1}) determined by the H_I galaxy masses and the relation in Wang et al. (2016), and R_{200} , versus total halo mass for SIMBA galaxies in each redshift snapshot. The running median for each redshift is given by the bold lines.

of the plot space) from the 1:1 relation line; that is, they have lower dark matter velocity dispersion measures when only considering $\sigma_{\text{DM-H1}}$. This particular result is entirely expected, as the velocity dispersion should naturally decrease when only considering a subset of dark matter particles in the galaxy halo.

The second effect, which was not expected, is that redshift evolution is much more pronounced, even for discy galaxies when considering spectral line width measures. This is evident both visually and when considering the y-intercept for the full sample between z = 0 and 1, which can differ by $\sim 3\sigma$. This suggests that there is some difference in the dark matter distribution within the baryon extent in SIMBA galaxies based on host galaxy morphology, which is less apparent from H I spectral line profiles when considering the entire galaxy dark matter halo. None the less, the redshift evolution in the y-intercept remains strongest when using V_{flat} . The slope does not evolve.

3.5 Velocity versus dark matter halo mass

Lastly, we consider how well each velocity measure corresponds with the dark matter halo mass, M_{DMH} . As before, we repeat the nine-panel plot for this relation in Fig. 10. Once again, V_{flat} has the least scatter but the flattest slope, and therefore is less correlated with M_{DMH} than spectral line width measures. Furthermore, spectral line width measures show a bigger distinction between the discy subsamples from all galaxies, and at fixed dark matter halo masses, galaxies rotate faster at lower redshifts. These results are consistent with the findings from the previous two figures, and the strong correlation between dark matter velocity dispersion and dark matter halo mass (Zahid et al. 2018). We do, however, note that this sample, which matches the expected number of galaxies to be detected by LADUMA, and hence designed to be a prediction of what LADUMA will find, is limited in number - a bigger sample may find a different result. Wider field surveys such as MIGHTEE-HI and WALLABY will better address this, but will also not extend to as high a redshift ($z \approx$ 1) as LADUMA.

The relation of M_{DMH} with line width is remarkably redshift invariant. Any redshift evolution is hard to distinguish from the spectral line width measurements (within 1σ in the difference of slope *m*). Noting the lower numbers for the discy subsample, a redshift evolution effect is slightly more apparent for all velocity measures (within $2\sigma-3\sigma$ in slope), albeit still slight, with convergence at the lower mass end when using $W_{50}/2$ and $W_{20}/2$. This means that, up to a redshift (*z*) of 1 at least, the H_I spectral line width can be used to get a reasonable estimate of the dark matter halo mass. This is particularly valuable since it is difficult to estimate dark matter halo masses in any other way for moderate-mass galaxies at these redshifts.

 Table 3. As in Table 2, but for the dark matter velocity dispersion when considering dark matter particles out to a distance determined by the H1 mass-size relation (Fig. 8).

Velocity definition	Redshift	Sample size	т	b	σ_{\perp}
Full sample					
V _{flat}	0	1043	0.75 ± 0.01	$0.80~\pm~0.01$	$0.027~\pm~0.001$
V _{flat}	0.5	559	0.78 ± 0.02	0.57 ± 0.03	0.031 ± 0.002
V_{flat}	1	180	0.71 ± 0.03	0.59 ± 0.06	0.039 ± 0.012
W ₅₀ /2	0	1043	1.04 ± 0.02	0.24 ± 0.03	0.064 ± 0.003
$W_{50}/2$	0.5	559	0.99 ± 0.03	0.15 ± 0.05	$0.077~\pm~0.004$
$W_{50}/2$	1	180	$0.97~\pm~0.06$	0.08 ± 0.11	0.095 ± 0.013
W ₂₀ /2	0	1043	0.98 ± 0.01	0.46 ± 0.02	0.046 ± 0.001
W ₂₀ /2	0.5	559	0.97 ± 0.02	0.33 ± 0.04	0.054 ± 0.003
$W_{20}/2$	1	180	0.99 ± 0.03	$0.20~\pm~0.07$	0.061 ± 0.005
Discy galaxy subsample ($\kappa_{rot} > 0.7$)					
V _{flat}	0	204	0.79 ± 0.01	0.74 ± 0.02	0.030 ± 0.002
V _{flat}	0.5	86	0.87 ± 0.02	$0.42~\pm~0.05$	$0.027~\pm~0.001$
V_{flat}	1	34	$0.74~\pm~0.05$	0.56 ± 0.10	0.032 ± 0.008
W ₅₀ /2	0	204	0.77 ± 0.02	0.80 ± 0.03	0.062 ± 0.002
$W_{50}/2$	0.5	86	0.83 ± 0.06	0.59 ± 0.11	$0.081~\pm~0.008$
$W_{50}/2$	1	34	$0.73~\pm~0.05$	0.75 ± 0.11	0.049 ± 0.016
W ₂₀ /2	0	204	0.78 ± 0.01	0.85 ± 0.02	0.035 ± 0.001
$W_{20}/2$	0.5	86	0.81 ± 0.03	0.69 ± 0.07	0.063 ± 0.006
W ₂₀ /2	1	34	$0.74~\pm~0.03$	0.79 ± 0.06	0.040 ± 0.005



Figure 10. As in Fig. 7, but plotting rotational velocity against the dark matter halo mass for the entire galaxy. The deviation from the best-fitting line is evident for $W_{50}/2$ at lower masses. Only weak redshift evolution can be seen.

Table 4 gives the best-fitting parameters for individual redshift snapshots for the full sample and discy subsamples for all velocity measures, as in previous measures. Given the redshift invariance, we additionally give the best-fitting parameters for galaxies combined across all three redshift snapshots for $W_{20}/2$ (chosen due to its reduced scatter compared to $W_{50}/2$), for the full sample:

$$\log_{10} \left(W_{20}/2 \right) = 0.24 \log_{10} \left(M_{\rm DMH} \right) - 0.52,\tag{3}$$

where $W_{20}/2$ is in units of km s⁻¹ and M_{DMH} in M_{\odot}, and the discy subsample:

$$\log_{10} \left(W_{20}/2 \right) = 0.21 \log_{10} \left(M_{\rm DMH} \right) - 0.12. \tag{4}$$

While the slopes are similar between these two samples, the discy subsample has a higher y-intercept (different to about 4σ). These relations can be used in upcoming HI emission surveys across all SKA pathfinder telescopes.

4 DISCUSSION

As established in Section 1, the BTFR provides a tight relation between the mass of the stars and gas with the rotation speed of spiral galaxies. The tightness of the relation across many orders of magnitude suggests a deep connection between the baryonic content and their dark matter haloes. Thus, it is important to consider how does this relation evolve with redshift. Redshift evolution

Table 4. As in Table 2, but for the dark matter halo mass (Fig.	10). We add additional best-fitting parameters for $W_{20}/2$ across all
three redshift snapshots, for the full sample and discy subsample.	

Velocity definition	Redshift	Sample size	т	b	σ_{\perp}
Full sample					
V _{flat}	0	1043	0.15 ± 0.01	0.35 ± 0.03	0.057 ± 0.001
V_{flat}	0.5	559	0.17 ± 0.01	0.14 ± 0.05	0.053 ± 0.001
V_{flat}	1	179	0.16 ± 0.02	0.16 ± 0.09	0.069 ± 0.003
W ₅₀ /2	0	1043	0.26 ± 0.01	-0.85 ± 0.05	0.095 ± 0.001
$W_{50}/2$	0.5	559	0.25 ± 0.01	-0.79 ± 0.07	0.102 ± 0.001
$W_{50}/2$	1	179	$0.25~\pm~0.02$	-0.86 ± 0.16	0.132 ± 0.002
W ₂₀ /2	0	1043	0.23 ± 0.01	-0.50 ± 0.04	0.071 ± 0.001
$W_{20}/2$	0.5	559	0.24 ± 0.01	-0.55 ± 0.06	0.069 ± 0.001
$W_{20}/2$	1	179	$0.22~\pm~0.03$	-0.30 ± 0.12	0.093 ± 0.001
W ₂₀ /2	All	1782	$0.24~\pm~0.01$	-0.52 ± 0.05	0.074 ± 0.001
Discy galaxy subsample ($\kappa_{rot} > 0.7$)					
V _{flat}	0	204	0.19 ± 0.01	-0.05 ± 0.09	0.064 ± 0.002
V _{flat}	0.5	86	0.18 ± 0.01	-0.03 ± 0.09	0.065 ± 0.008
V _{flat}	1	33	$0.20~\pm~0.02$	-0.21 ± 0.21	0.059 ± 0.007
W ₅₀ /2	0	204	0.19 ± 0.01	-0.08 ± 0.13	0.087 ± 0.002
$W_{50}/2$	0.5	86	0.20 ± 0.02	-0.09 ± 0.19	0.110 ± 0.007
$W_{50}/2$	1	33	0.23 ± 0.02	-0.43 ± 0.20	0.067 ± 0.014
$W_{20}/2$	0	204	0.19 ± 0.01	0.07 ± 0.08	0.059 ± 0.001
$W_{20}/2$	0.5	86	0.20 ± 0.01	-0.04 ± 0.16	0.088 ± 0.007
$W_{20}/2$	1	33	$0.23\ \pm\ 0.03$	-0.38 ± 0.29	0.068 ± 0.016
W ₂₀ /2	All	323	0.21 ± 0.01	-0.12 ± 0.12	0.073 ± 0.003

of any form of the TFR, as summarized in Section 3.2.3 where we compare our results with the literature, has been an area of debate in observational and simulated studies covering various methods of rotational measurement, although studies considering measures such as W_{20} of H I emission profiles in simulated galaxies (Obreschkow et al. 2009a) did observe redshift evolution of the BTFR.

Previous observational studies specifically using the H I 21-cm transition in emission have been limited to lower redshift due to the weakness of the signal. Upcoming H I emission surveys with SKA pathfinder telescopes will probe previously unexplored redshift regimes, with LADUMA (the deepest of these surveys) aiming to go redshifts (z) of \gtrsim 1. It is hence expected that LADUMA may be able to present evidence of an evolution of the BTFR, which indeed is one of its science goals. Our study of a sample of simulated galaxies from the SIMBA hydrodynamic simulation, which has similar sample size and mass range of galaxies to the predicted sample from LADUMA, shows that LADUMA will be able to measure such a redshift evolution, although we emphasize the need for LADUMA to discern discy galaxies through ancillary information.

The $W_{20}/2$ spectral line width measure shows this evolution most clearly, both in the slope and in the *y*-intercept, between z = 0and 1. V_{flat} also showcases redshift evolution, albeit this measure from rotation curves will not be applicable at high redshift as galaxies will not be spatially resolved, and hence such measures will be impossible. From the spectral line width measures, which agree visually with the trend seen with σ_{DM} , we find that at equal baryonic masses, higher redshift galaxies rotate faster. This assumes that such galaxies within SIMBA are realistic representations of true galaxies, and that additional effects such as random inclinations of disc galaxies and any potential difficulty in obtaining accurate measures of this and stellar mass-to-light ratios of LADUMA galaxies do not significantly affect the LADUMA study – see the end of Section 3.2.2 for further details. It is also noted that low numbers of discy galaxies are available at higher redshift, resulting in larger errors and a lack of low-mass galaxies, hence introducing a bias towards higher mass galaxies. While this sample distribution is expected to occur in LADUMA (Section 2.1), it is an important point to consider. Larger samples than what will be possible with LADUMA, such as with the SKA itself, or with SKA pathfinder telescopes at lower redshift than LADUMA, may indeed discover different trends if they also probe to lower baryonic masses or greater numbers. The SIMBA simulation also excludes galaxies with stellar masses below our mass resolution limit, although we do not expect many galaxies below this mass limit of $7.25 \times 10^8 M_{\odot}$ to be detected in H1 by LADUMA.

We also show that, with a SIMBA sample chosen to represent LADUMA, there exists a mild redshift evolution of the *y*intercept of the relation between the rotational velocity and σ_{DM} of the full dark matter halo, while stronger evolution is evident when only considering the σ_{DM} of dark matter particles within the same extent as the baryonic matter. Again, other HI galaxy samples to LADUMA that probe a different parameter space in redshift and galaxy mass may give a different evolution. A lack of redshift evolution between observational rotational velocity and the dark matter halo mass, meanwhile, showcases the potential of upcoming HI emission surveys in estimating the dark matter halo mass, which is a finding we make in addition to our BTFR analysis.

5 CONCLUSIONS

We have examined three common rotational velocity measures from galaxy rotation curves, using the methodology presented in Glowacki et al. (2020), and H_I spectral line widths by creating H_I data cubes through MARTINI, for SIMBA-hires galaxies. With each measure, we consider the redshift evolution of the BTFR to predict the results of this study to be undertaken by the LADUMA survey with the MeerKAT array. We then compare each measure with the dark matter velocity dispersion (σ_{DM}), from both the host galaxy's dark matter halo and particles within the same extent as the baryonic mass (σ_{DM-HI}), and the dark matter halo mass. The redshift evolution of these trends is hence also predicted for LADUMA.

We find that our spectral line measures follow a 1:1 relation with V_{flat} . We note that a downturn in this relation seen for low-mass (or slowly rotating) galaxies is attributed to dispersion-dominated galaxies, which is removed when we only consider the discy subsample. This selection proves crucial in the redshift evolution of the BTFR as well, which observationally only holds for discy galaxies that are kinematically dominated in their rotation. We find a weak redshift evolution of the BTFR between z = 0 and 1 when using σ_{DM} and W_{20} – at fixed velocities, the baryonic mass of galaxies decreases with increasing redshift (z = 0-1). When fixing the slope from the z = 0 best BTFR fit, the y-intercept decreases with redshift for all measures, except for V_{flat} that instead increases. Spectral line width measures such as W_{20} are also preferred over narrower measures, e.g. W_{50} , due to reduced scatter. LADUMA will need to identify the morphologies of the host galaxies to best study the redshift evolution of the BTFR.

When comparing observational rotational velocity measures with $\sigma_{\rm DM}$, we find that redshift evolution is stronger when using $V_{\rm flat}$ and galaxies of various morphologies, rather than from spectral line widths and the discy galaxy subsample, suggesting that the measured $\sigma_{\rm DM}$ change with redshift is dependent on the host galaxy morphology. This redshift evolution from $V_{\rm flat}$ can explain the apparent 'reverse' trend found for this observational redshift measure in the BTFR with redshift.

However, the dark matter velocity dispersion of particles within the same extent as the H I gas from the galaxy's centre of mass $(\sigma_{\text{DM-HI}})$ displays far clearer redshift evolution in both the full and discy samples for all velocity measures. At higher redshifts, galaxies have a lower rotational velocity at fixed σ_{DM} . W_{20} again gives a tighter relation here than W_{50} , and while we note V_{flat} is tighter still, this observational measure is not feasible for LADUMA at higher redshifts due to insufficient spatial resolution.

Weak redshift evolution is seen between the velocity measures and the dark matter halo mass. From the best-fitting values, similar slope values *m* are seen between the full sample and discy subsample, with the *y*-intercept *b* being higher in the discy subsample. We give fits for individual redshift snapshots for all rotational velocity measures, and for $W_{20}/2$ across z = 0-1 from our three snapshots combined for this relation. These fits can hence be used to estimate the dark matter halo mass from HI spectral line profile widths with upcoming SKA pathfinder telescope HI emission surveys.

SIMBA has proved instrumental in studying the BTFR, with good comparison with the SPARC survey shown in Glowacki et al. (2020), and exciting predictions for the LADUMA survey made here. The ability to trace the dynamics of galaxies out to intermediate redshifts using HI spectral line widths thus provides interesting dynamical information for both galaxies and haloes, even without resolving the rotation curves. As explorations of the HI universe enter into a new era, spectral line widths promise to provide a key new piece of observational data to explore galaxy evolution and constrain galaxy formation models.

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author. SIMBA snapshots and galaxy catalogues used for this work can be found at http://simba.roe.ac.uk/.

REFERENCES

- Abril-Melgarejo V. et al., 2021, A&A, 647, A152
- Appleby S., Davé R., Kraljic K., Anglés-Alcázar D., Narayanan D., 2019, MNRAS, 494, 6053
- Bamford S. P., Aragón-Salamanca A., Milvang-Jensen B., 2006, MNRAS, 366, 308
- Barden M., Lehnert M. D., Tacconi L., Genzel R., White S., Franceschini A., 2003, preprint (astro-ph/0302392)
- Blyth S. et al., 2016, Proc. Sci., LADUMA: Looking at the Distant Universe with the MeerKAT Array. SISSA, Trieste, PoS#4
- Broeils A. H., Rhee M. H., 1997, A&A, 324, 877
- Brook C. B., Santos-Santos I., Stinson G., 2016, MNRAS, 459, 638
- Darling J., Macdonald E. P., Haynes M. P., Giovanelli R., 2011, ApJ, 742, 60
- Davé R., Anglés-Alcázar D., Narayanan D., Li Q., Rafieferantsoa M. H., Appleby S., 2019, MNRAS, 486, 2827
- Davé R., Crain R. A., Stevens A. R. H., Narayanan D., Saintonge A., Catinella B., Cortese L., 2020, MNRAS, 497, 146
- Deboer B. D. R. et al., 2009, Proc. IEEE, 97, 1507
- de Rossi M. E., Tissera P. B., Pedrosa S. E., 2010, A&A, 519, A89
- Fernández Lorenzo M., Cepa J., Bongiovanni A., Castañeda H., Pérez García A. M., Lara-López M. A., Pović M., Sánchez-Portal M., 2009, A&A, 496, 389
- Foreman-Mackey D., Hogg D. W., Lang D., Goodman J., 2013, PASP, 125, 306
- Giovanelli R., Haynes M. P., 2002, ApJ, 571, L107
- Glowacki M., Elson E., Davé R., 2020, MNRAS, 498, 3687
- Gurovich S., Freeman K., Jerjen H., Staveley-Smith L., Puerari I., 2010, AJ, 140, 663
- Haardt F., Madau P., 2012, ApJ, 746, 125
- Haynes M. P., Giovanelli R., Chamaraux P., da Costa L. N., Freudling W., Salzer J. J., Wegner G., 1999, AJ, 117, 2039
- Holwerda B. W., Blyth S. L., Baker A. J., 2012, in Tuffs R. J., Popescu C. C., eds, Proc. IAU Symp. 284, The Spectral Energy Distribution of Galaxies – SED 2011. Kluwer, Dordrecht, p. 496
- Hopkins P. F., 2015, MNRAS, 450, 53

- Jarvis M. J. et al., 2017, Proc. Sci., The MeerKAT International GHz Tiered Extragalactic Exploration (MIGHTEE) Survey. SISSA, Trieste, PoS#6
- Jonas J., MeerKAT Team, 2016, Proc. Sci., The MeerKAT Radio Telescope. SISSA, Trieste, PoS#1
- Koribalski B. S. et al., 2020, Ap&SS, 365, 118
- Lelli F., McGaugh S. S., Schombert J. M., 2016, ApJ, 816, L14
- Lelli F., McGaugh S. S., Schombert J. M., Desmond H., Katz H., 2019, MNRAS, 484, 3267
- McGaugh S. S., 2012, AJ, 143, 40
- Maddox N. et al., 2021, A&A, 646, A35
- Meyer M., 2009, Proc. Sci., Exploring the HI Universe with ASKAP. SISSA, Trieste, PoS#15
- Meyer M. et al., 2004, MNRAS, 350, 1195
- Noordermeer E., Verheijen M. A. W., 2007, MNRAS, 381, 1463
- Noordermeer E., van der Hulst J. M., Sancisi R., Swaters R. A., van Albada T. S., 2005, A&A, 442, 137
- Obreschkow D., Croton D., De Lucia G., Khochfar S., Rawlings S., 2009a, ApJ, 698, 1467
- Obreschkow D., Klöckner H. R., Heywood I., Levrier F., Rawlings S., 2009b, ApJ, 703, 1890
- Planck Collaboration XIII, 2016, A&A, 594, A13
- Ponomareva A. A., Verheijen M. A. W., Peletier R. F., Bosma A., 2017, MNRAS, 469, 2387
- Ponomareva A. A., Verheijen M. A. W., Papastergis E., Bosma A., Peletier R. F., 2018, MNRAS, 474, 4366
- Portinari L., Sommer-Larsen J., 2007, MNRAS, 375, 913
- Puech M. et al., 2008, A&A, 484, 173
- Puech M., Hammer F., Flores H., Delgado-Serrano R., Rodrigues M., Yang Y., 2010, A&A, 510, A68

- Rahmati A., Pawlik A. H., Raicevic M., Schaye J., 2013, MNRAS, 430, 2427
- Sales L. V., Navarro J. F., Theuns T., Schaye J., White S. D. M., Frenk C. S., Crain R. A., Dalla Vecchia C., 2012, MNRAS, 423, 1544
- Sales L. V. et al., 2017, MNRAS, 464, 2419
- Sanders R. H., McGaugh S. S., 2002, ARA&A, 40, 263
- Sommer-Larsen J., Götz M., Portinari L., 2003, ApJ, 596, 47
- Springel V., 2005, MNRAS, 364, 1105
- Springob C. M., Masters K. L., Haynes M. P., Giovanelli R., Marinoni C., 2007, ApJ, 172, 599
- Swaters R. A., van Albada T. S., van der Hulst J. M., Sancisi R., 2002, A&A, 390, 829
- Thomas N., Dave R., Jarvis M. J., Angles-Alcazar D., 2020, MNRAS, 503, 3492
- Tiley A. L. et al., 2019, MNRAS, 482, 2166
- Tully R. B., Fisher J. R., 1977, A&A, 500, 105
- Übler H. et al., 2017, ApJ, 842, 121
- Verheijen M. A. W., Sancisi R., 2001, A&A, 370, 765
- Vogt N. P., 2007, in Combes F., Palouš J., eds, Proc. IAU Symp. 235, Galaxy Evolution across the Hubble Time. Cambridge Univ. Press, Cambridge, p. 3
- Wang J., Koribalski B. S., Serra P., van der Hulst T., Roychowdhury S., Kamphuis P., Chengalur J. N., 2016, MNRAS, 460, 2143
- Zahid H. J., Sohn J., Geller M. J., 2018, ApJ, 859, 96
- Zaritsky D. et al., 2014, AJ, 147, 134

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